

Teaching PRA and conducting PRA research at universities

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PRA Methodology

- **What universities can teach**
 - Probability
 - Statistics
 - PRA structure and models
 - PRA calculations
 - Risk management process and safety goals
- **What they cannot teach**
 - Accident sequence development

Probability and Statistics

- U.S. nuclear and mechanical engineers do not, in general, have a background in probability and statistics
- An introductory PRA course must cover the essentials of probability and statistics
- Doing so limits the time for teaching PRA methods
- Topics specific to PRA
 - Bayesian methods
 - Aleatory and epistemic uncertainties
 - However, there is only one kind of uncertainty
 - Importance measure
- Practitioners are uncomfortable defending their judgment (as opposed to classical statistics)

The Model of the “World”

- Deterministic, e.g., a mechanistic computer code
- Probabilistic (*Aleatory*) model,
e.g., $R(t/\lambda) = \exp(-\lambda t)$
- Both deterministic and aleatory models of the world have assumptions and parameters.
- How confident are we about the validity of these assumptions and the numerical values of the parameters?

Epistemic Model

- Uncertainties in assumptions are not handled routinely. If necessary, sensitivity studies are performed.
- Parameter uncertainties are reflected on appropriate **epistemic** distributions.
- For the failure rate:

$\pi(\lambda)$
- $\pi(\lambda)d\lambda = \text{Pr}(\text{the failure rate has a value in } d\lambda \text{ about } \lambda)$

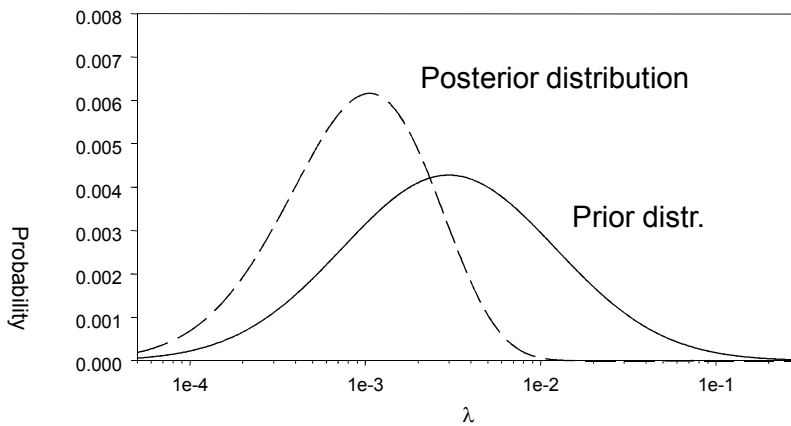
WASH-1400 Failure Rates

Component/Primary Failure Modes	Assessed Values	
	Lower Bound	Upper Bound
Mechanical Hardware		
Pumps		
Failure to start, Q_d :	$3 \times 10^{-4}/d$	$3 \times 10^{-3}/d$
Failure to run, λ_o : (Normal Environments)	$3 \times 10^{-6}/hr$	$3 \times 10^{-4}/hr$
Valves		
Motor Operated		
Failure to operate, Q_d :	$3 \times 10^{-4}/d$	$3 \times 10^{-3}/d$
Plug, Q_d :	$3 \times 10^{-5}/d$	$3 \times 10^{-4}/d$
Solenoid Operated		
Failure to operate, Q_d :	$3 \times 10^{-4}/d$	$3 \times 10^{-3}/d$
Plug, Q_d :	$3 \times 10^{-5}/d$	$3 \times 10^{-4}/d$
Air Operated		
Failure to operate, Q_d :	$1 \times 10^{-4}/d$	$1 \times 10^{-3}/d$
Plug, Q_d :	$3 \times 10^{-5}/d$	$3 \times 10^{-4}/d$
Check		
Failure to open, Q_d :	$3 \times 10^{-5}/d$	$3 \times 10^{-4}/d$
Relief		
Failure to open, Q_d :	$3 \times 10^{-6}/d$	$3 \times 10^{-5}/d$
Manual		
Plug, Q_d :	$3 \times 10^{-5}/d$	$3 \times 10^{-4}/d$
Pipe		
Plug/rupture		
≤ 3 " diameter, λ_o :	$3 \times 10^{-11}/hr$	$3 \times 10^{-8}/hr$
> 3 " diameter, λ_o :	$3 \times 10^{-12}/hr$	$3 \times 10^{-9}/hr$
Clutches		
Mechanical		
Failure to engage/disengage	$1 \times 10^{-4}/d$	$1 \times 10^{-3}/d$
Electrical Hardware		
Electrical Clutches		
Failure to operate, Q_d :	$1 \times 10^{-4}/d$	$1 \times 10^{-3}/d$

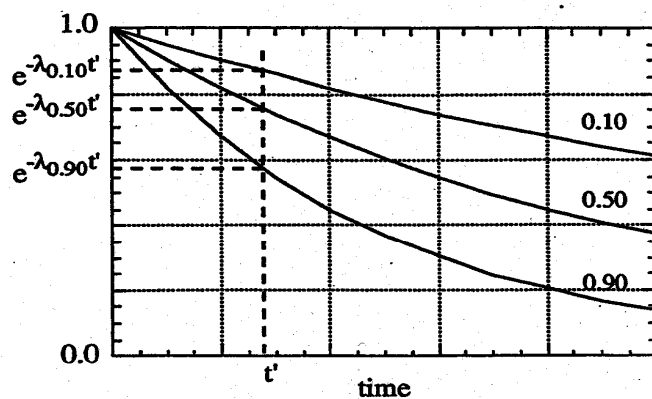
Example of Bayesian updating of epistemic distributions

Five components were tested for 100 hours each and no failures were observed.

$$\pi'(\lambda / E) = \frac{L(E / \lambda)\pi(\lambda)}{\int L(E / \lambda)\pi(\lambda)d\lambda}$$



Communication of Epistemic Uncertainties



Epistemic Correlation

- Consider two nominally identical isolation valves
- They share the epistemic distribution of failure rate

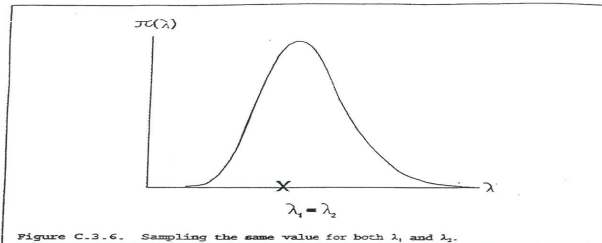


Figure C.3.6. Sampling the same value for both λ_1 and λ_2 .

$$Q = q^2 \quad , \quad a_Q = a_q^2 + \beta_q^2$$

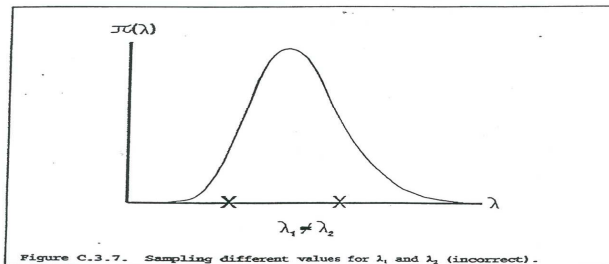
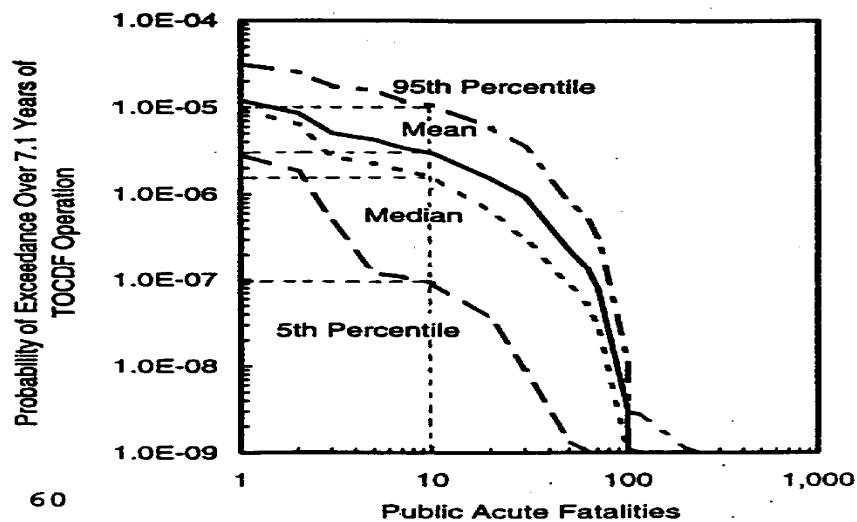


Figure C.3.7. Sampling different values for λ_1 and λ_2 (incorrect).

$$Q^* = q_1 q_2 \quad , \quad a_{q^*} = a_{q_1} a_{q_2} = a_q^2$$

Risk Curves

Propagating epistemic uncertainties through the PRA models (usually via Monte Carlo simulation), we produce the risk curves.



PRA Models

- **Event and fault trees**
- **Human reliability**
- **Reliability physics models**
- **Common-cause failures**
- **Examples from PRAs**
- **External events**

PRA Methodological Research

- **Data specialization using Bayes theorem**
- **Epistemic correlation of parameter distributions**
- **Plant-to-plant variability**
- **Fire methodology**
- **Human Reliability Analysis**
- **Uncertainties in phenomenological work**
- **Model uncertainty**
- **Safety goals**
- **Risk management**
- **Simulation methods**

Plant-to-Plant Variability

- **Suppose the evidence from two plants is**
 - (1 fire in 8 years) and
 - (0 fires in 6 years)
- **If we say that the evidence is (1 fire in 14 years), we will be increasing the strength of the evidence artificially resulting in a narrower distribution for the fire rate**
- **The evidence from the two plants must be processed separately so that the distribution will be broader**

Concluding Remarks

- **Teaching a course in PRA is usually hampered by the students' lack of background in probability and statistics**
- **Most students have been exposed to classical (frequentist) statistics; they have difficulty switching to Bayesian (subjectivist) statistics**
- **A PRA course is necessarily limited to methodology**
- **Ideally, traditional engineering courses would discuss uncertainties in their models.**